# 11.8 Videos Guide

## 11.8a

- Form of a power series
  - $\circ \quad \sum_{n=0}^{\infty} a_n x^n = a_0 + a_1 x + a_2 x^2 + a_3 x^3 + \cdots$

### Exercise:

• Find the radius and interval of convergence of  $\sum_{n=0}^{\infty} (x+2)^n$ .

# Theorem (statement):

- For a given power series  $\sum_{n=0}^{\infty} a_n (x-a)^n$ , there are only three possibilities:
  - (i) The series converges only for x = aR = 0; interval: {a}
  - (ii) The series converges for all  $x \in \mathbb{R}$  $R = \infty$ ; interval:  $(-\infty, \infty)$
  - (iii) There is a number R > 0 such that the series converges if |x a| < R and diverges if |x-a| > R

Note: Convergence at the endpoints of the interval is determined by testing them individually.

### Exercises:

Find the radius of convergence and interval of convergence of the series.

11.8b

• 
$$\sum_{n=1}^{\infty} \frac{(-1)^n x^n}{\sqrt[3]{n}}$$

- $\sum_{n=1}^{\infty} n^n x^n$   $\sum_{n=1}^{\infty} \frac{x^{2n}}{n!}$

# 11.8c

• 
$$\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{n5^n} x^n$$
  
•  $\sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)2^n} (x-1)^n$ 

11.8d  

$$\sum_{n=2}^{\infty} \frac{b^n}{\ln n} (x-a)^n, \quad b > 0$$

#### 11.8e

•  $\sum_{n=1}^{\infty} \frac{n! x^n}{1 \cdot 3 \cdot 5 \cdot \cdots \cdot (2n-1)}$